

Contour Forests: Fast Multi-threaded Augmented Contour Trees

Journée Visu
2017

Charles Gueunet, UPMC and Kitware

Pierre Fortin, UPMC

Julien Jomier, Kitware

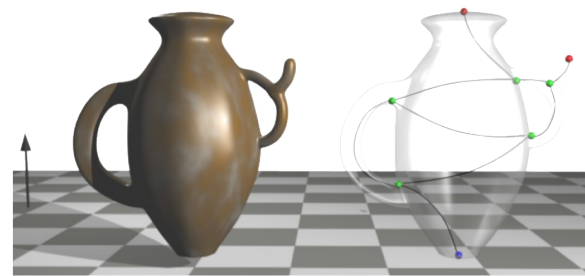
Julien Tierny, UPMC



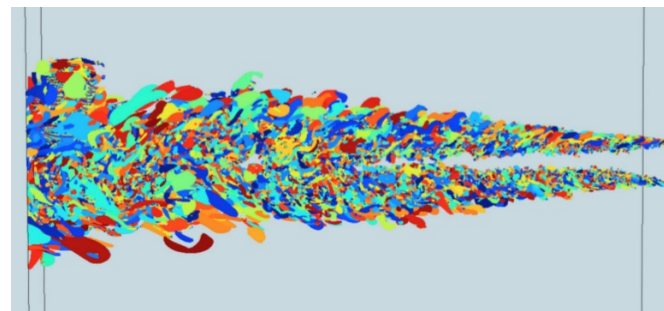
Introduction

- Context
- Related Works
- Challenges
- Contributions

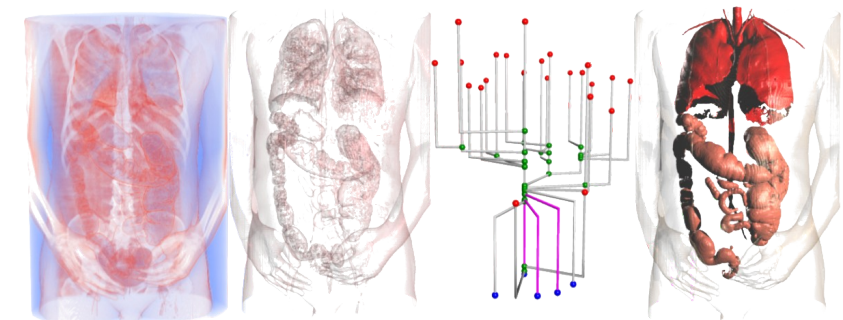
- Topological analysis: classical approach in Sci Viz
 - **Contour Trees**, Reeb Graphs, Morse-Smale Complexes...



[DoraiswamyTVCG13]



[LandgeSC14]

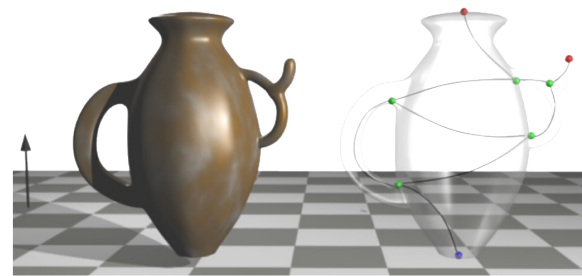


[MaadasamyHiPC12]

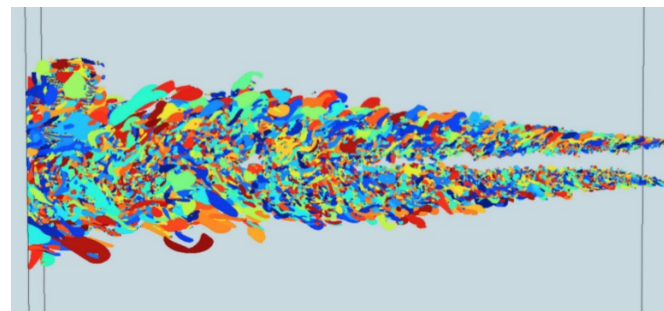
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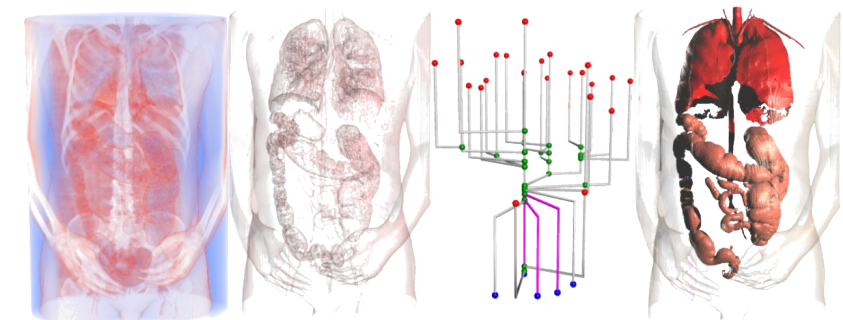
- Topological analysis: classical approach in Sci Viz
 - **Contour Trees**, Reeb Graphs, Morse-Smale Complexes...
 - Increasing data size and complexity
 - Challenge for interactive exploration
 - Multi-core architectures are common
- Motivation for multi-threaded parallelism



[DoraiswamyTVCG13]



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Sequential:

- [CarrSODA00,ChiangCG05]

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- [PascucciAlgorithmica04]

| Ref | CT | Tet. mesh | Augmented | Combination |
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- Topological data analysis algorithms
 - Intrinsically sequential approaches
 - Challenging parallelization

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- Topological data analysis algorithms
 - Intrinsically sequential approaches
 - Challenging parallelization
- Contour Tree:
 - No complete parallelization (only subroutines)
 - No efficient parallel algorithm for augmented trees

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- Efficient multi-threaded algorithm for contour tree computation
 - Simple approach
 - Good parallel efficiency on workstations

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- Efficient multi-threaded algorithm for contour tree computation
 - Simple approach
 - Good parallel efficiency on workstations
- Ready-to-use VTK-based C++ implementation: in TTK
 - Generic input (VTU/VTI, 2D/3D)
 - Generic output (augmented trees)

Summary

1) Introduction

2) Preliminaries

- Background
- Overview

3) Algorithm

- Domain partitioning
- Local computation
- Contour forest stitching

4) Experimental results

- Scalability
- Efficiency
- Limitations

5) Application

6) Conclusion

- Recall
- Perspective



Preliminaries

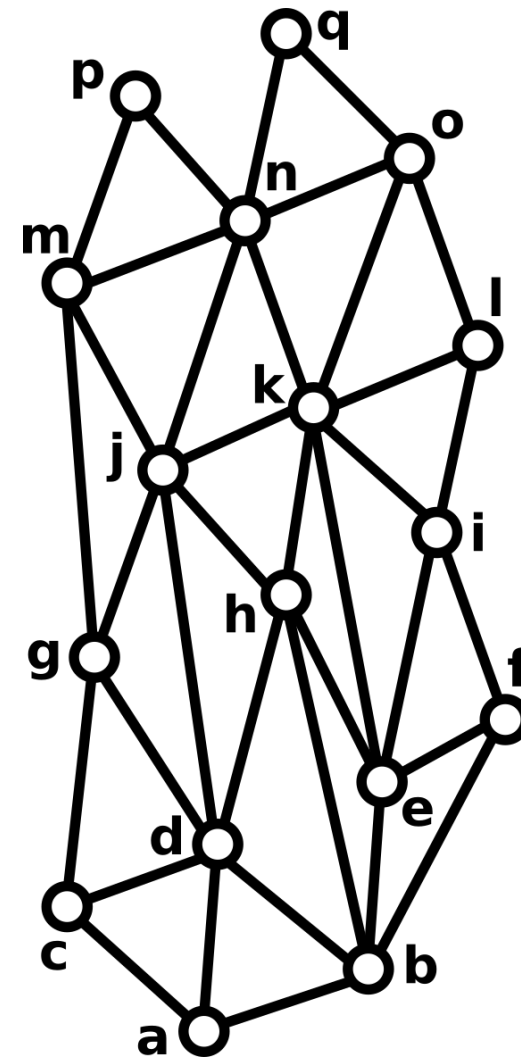
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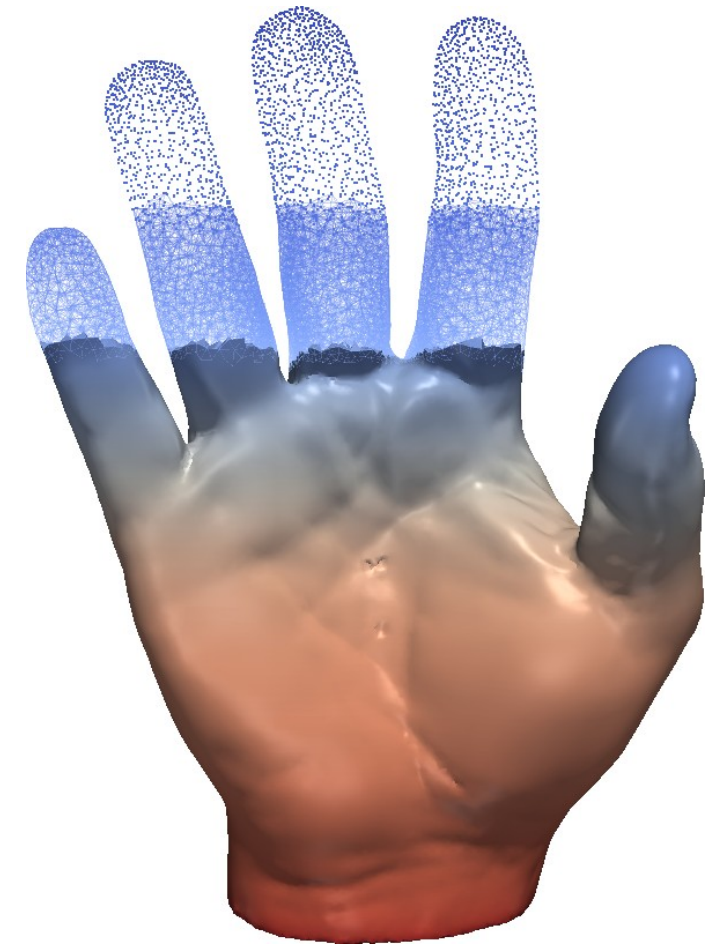
Input data:

- Piecewise linear scalar field

$$f : \mathcal{M} \rightarrow \mathbb{R}$$



2D Example



3D Example

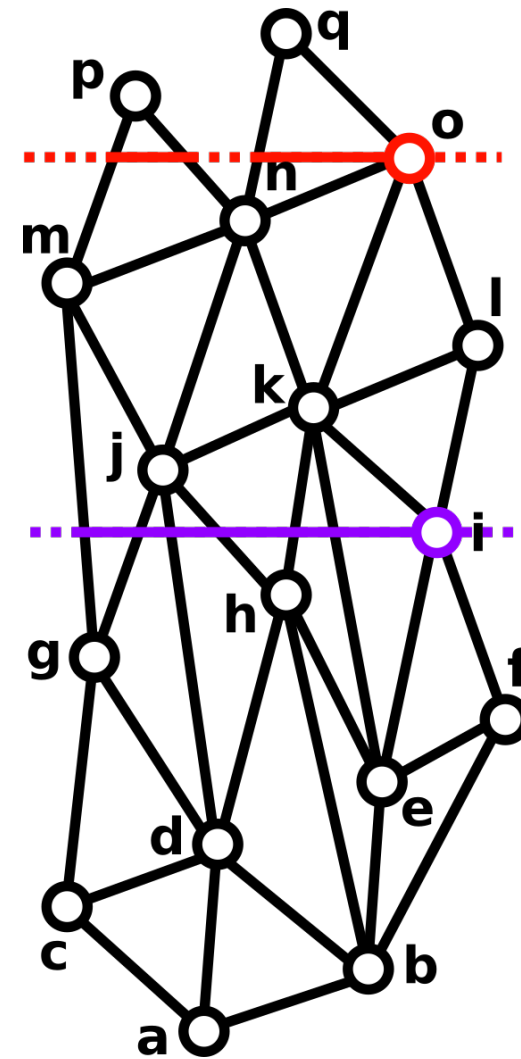
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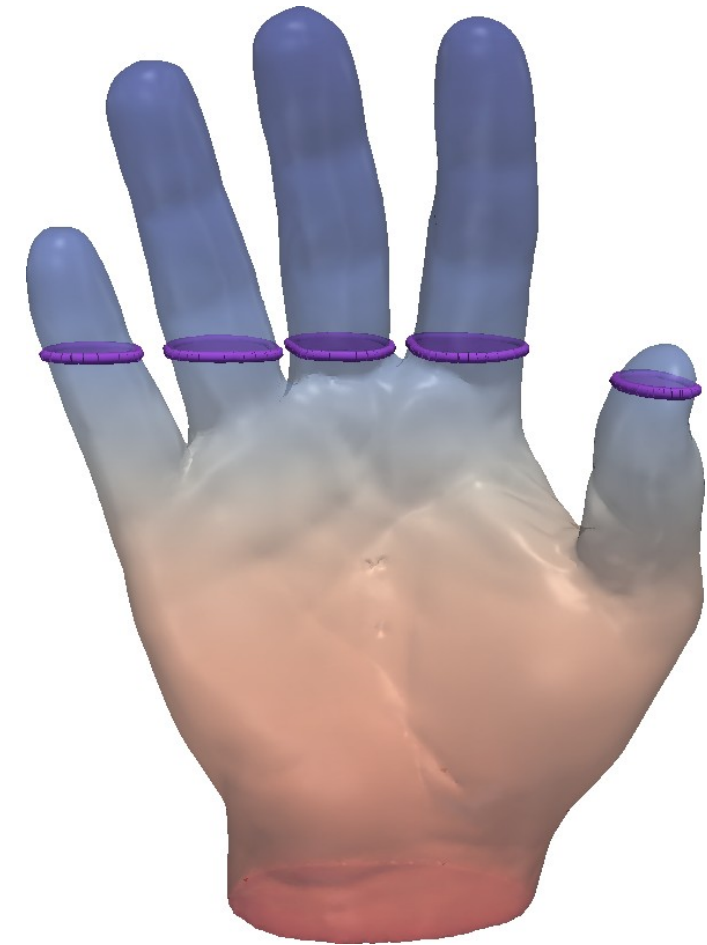
Level set:

- Preimage of a scalar value
- Isovalue: $i \in \mathbb{R}$ onto \mathcal{M}

$$f^{-1}(i) = \{p \in \mathcal{M} \mid f(p) = i\}$$



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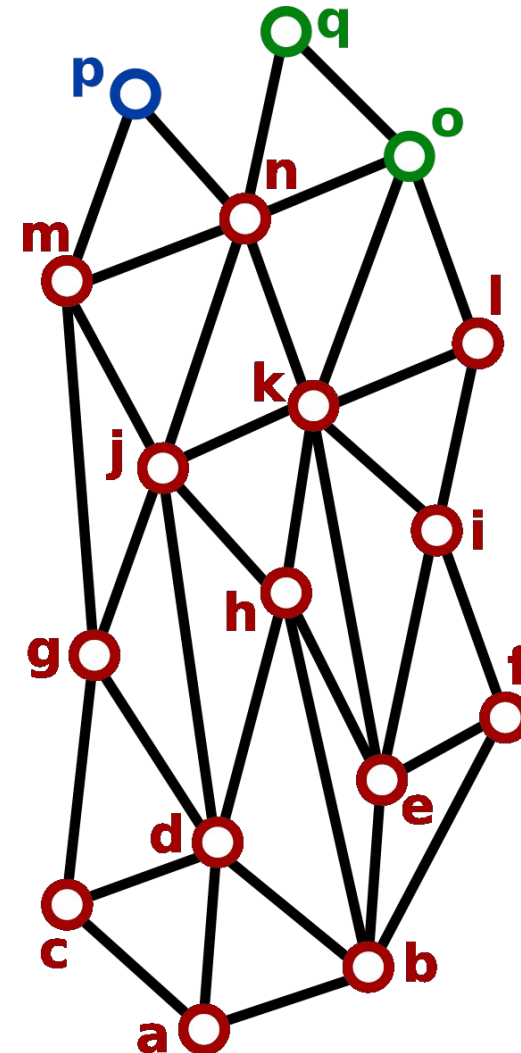
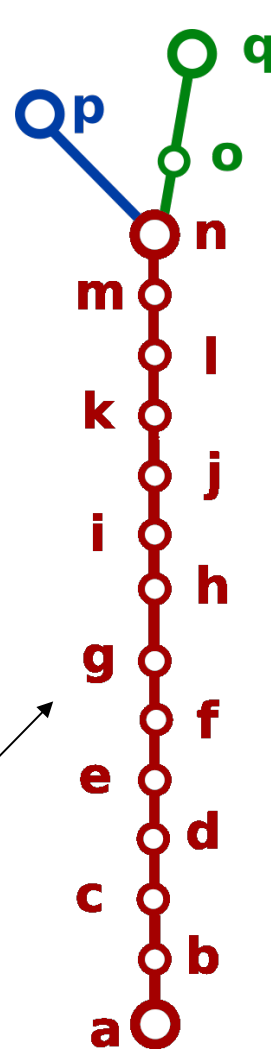
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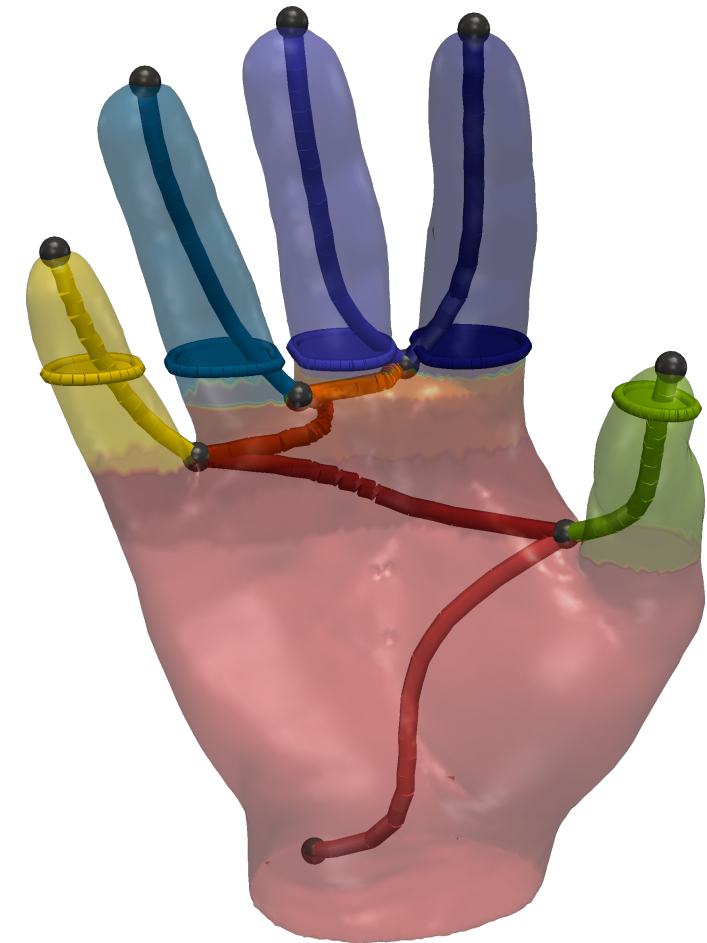
Contour tree:

- Simply connected input domain
- 1-dimensional simplicial complex

Regular vertices
in augmented tree



2D Example



3D Example

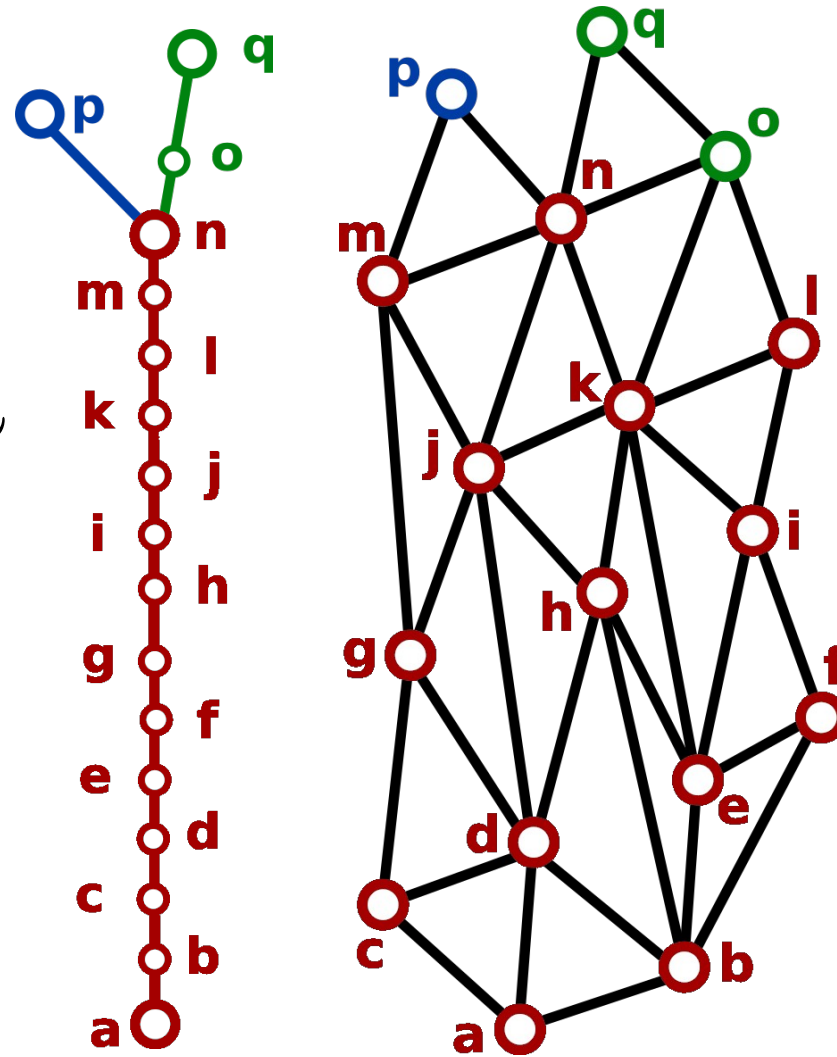
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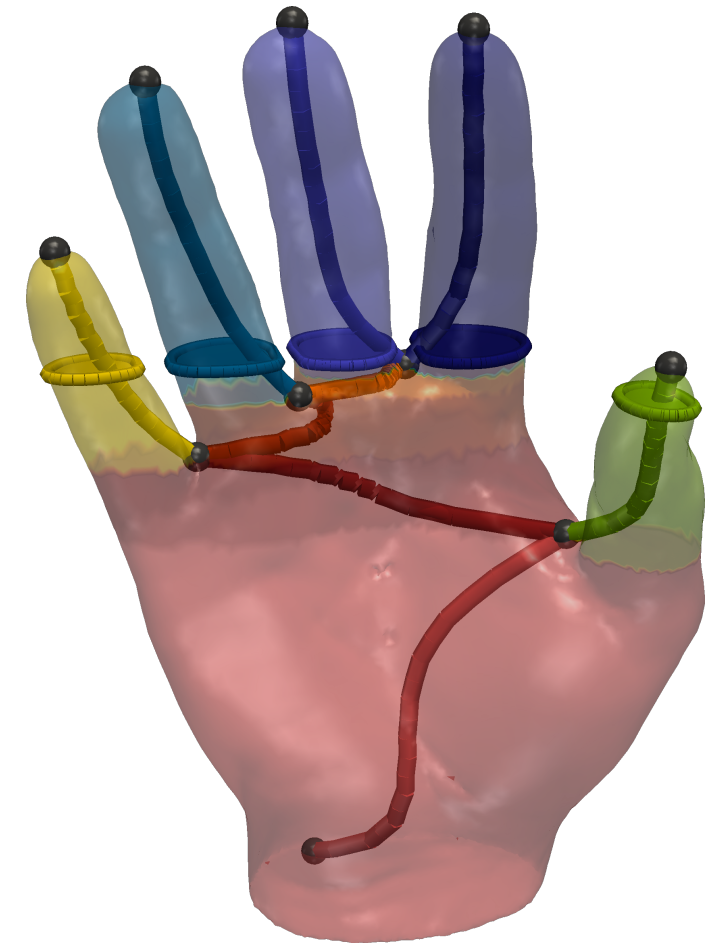
Contour tree:

- Quotient space: $\mathcal{C}(f) = \mathcal{M} / \sim$
- Equivalence relation: $p_1 \sim p_2$

$$\begin{cases} f(p_1) = f(p_2) \\ p_2 \in f^{-1}(f(p_1))_{p_1} \end{cases}$$



2D Example



3D Example

Preliminaries

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Main steps of our approach:

- 1) Sort vertices
- 2) Create partitions using level sets
- 3) Compute local trees
- 4) Stitch local trees

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Pros:

- Simple approach
- Local computation of CT
- Augmented trees
- Simple stitching of the forests

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Cons:

- Depends on interface level sets



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- Range driven partitions
- Sorted scalars \Rightarrow balanced partitions
- Use $n_t/2$ partitions

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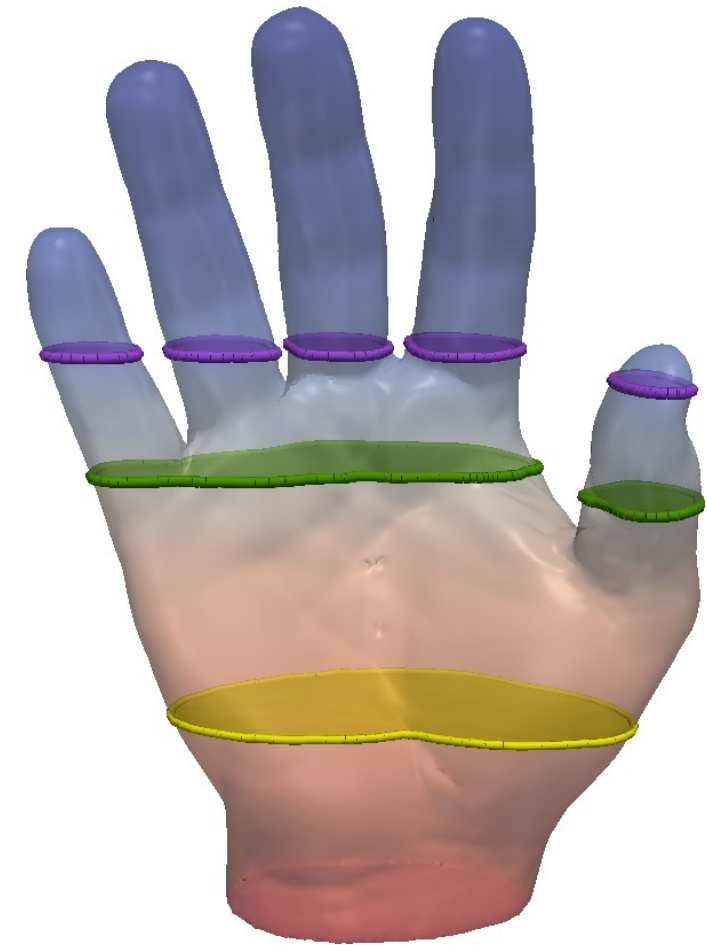
$$f(\mathcal{M}) = \mathcal{I}_0 \cup \mathcal{I}_1 \cup \dots \cup \mathcal{I}_{(n_t/2)-1}$$
$$|\sigma_0|_i \approx |\sigma_0|_j \quad \forall i \neq j$$

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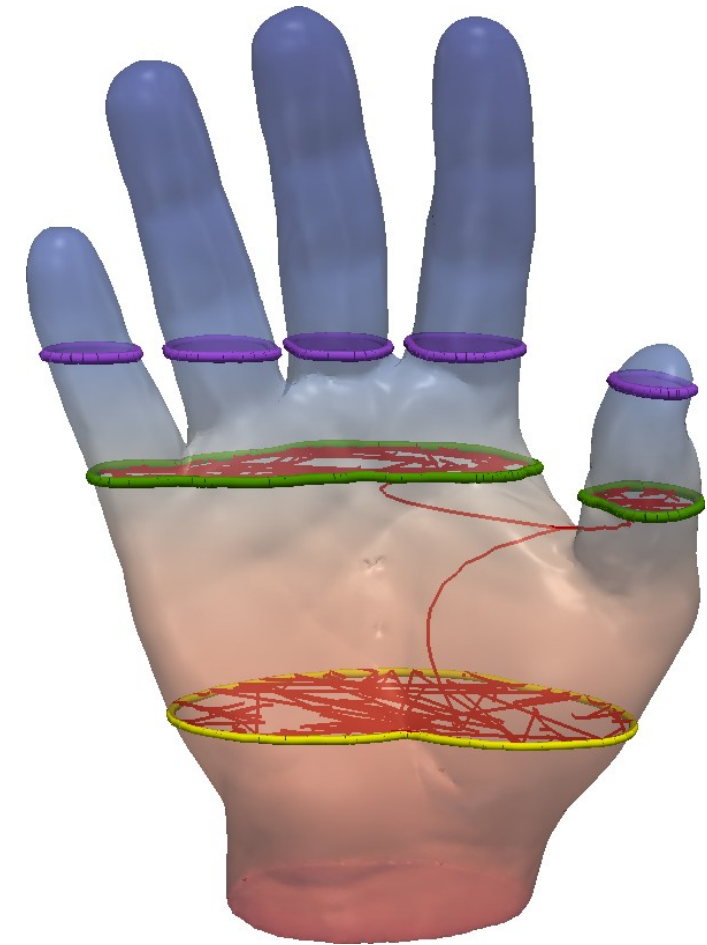
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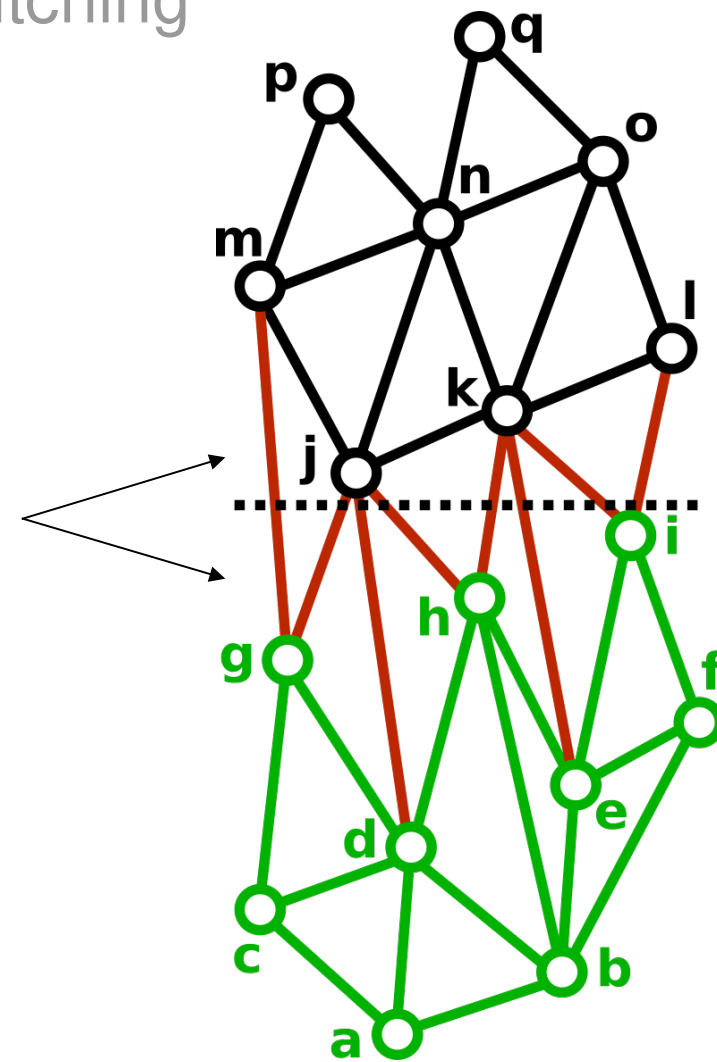
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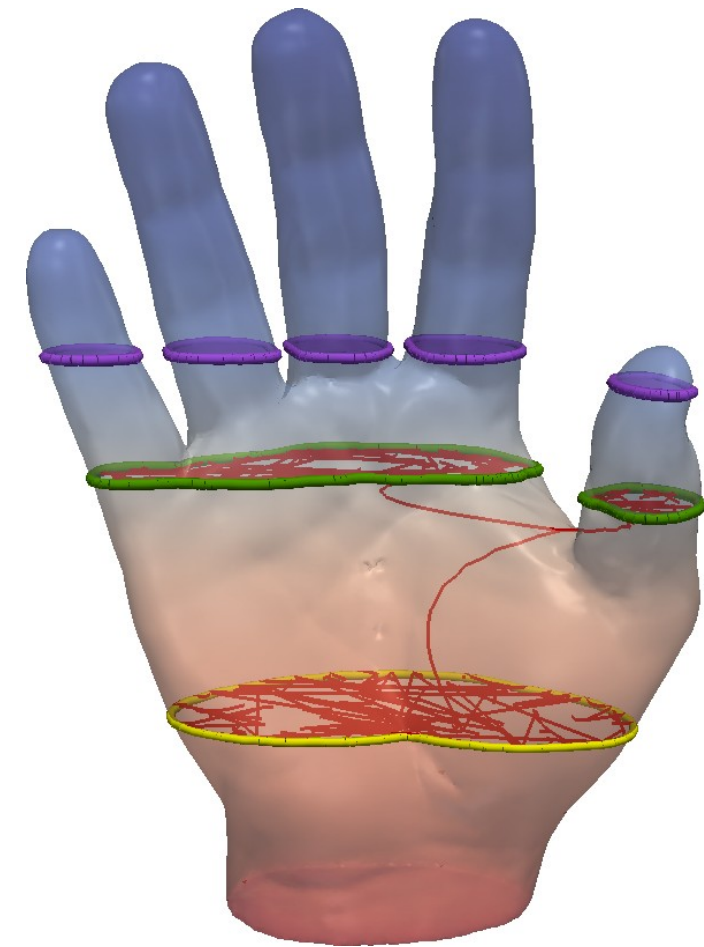
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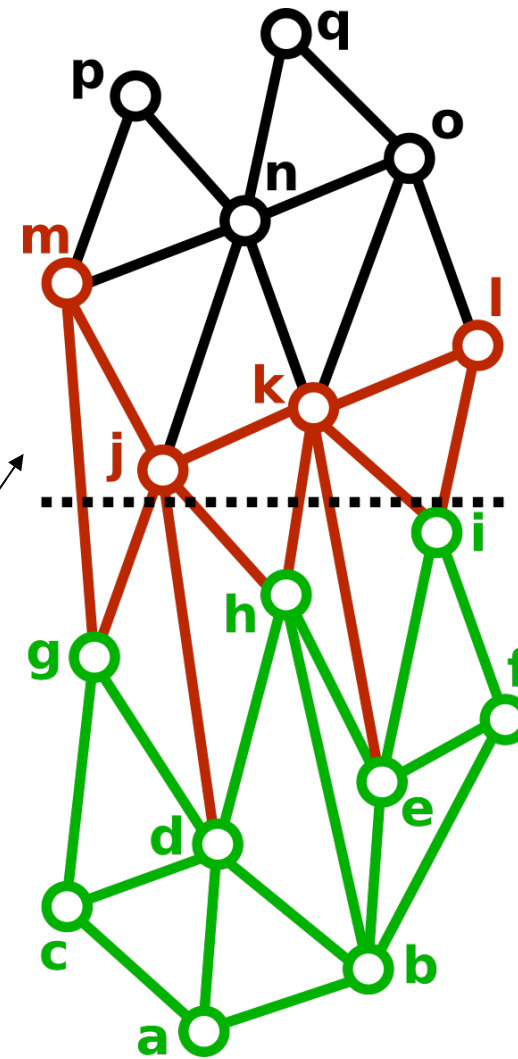
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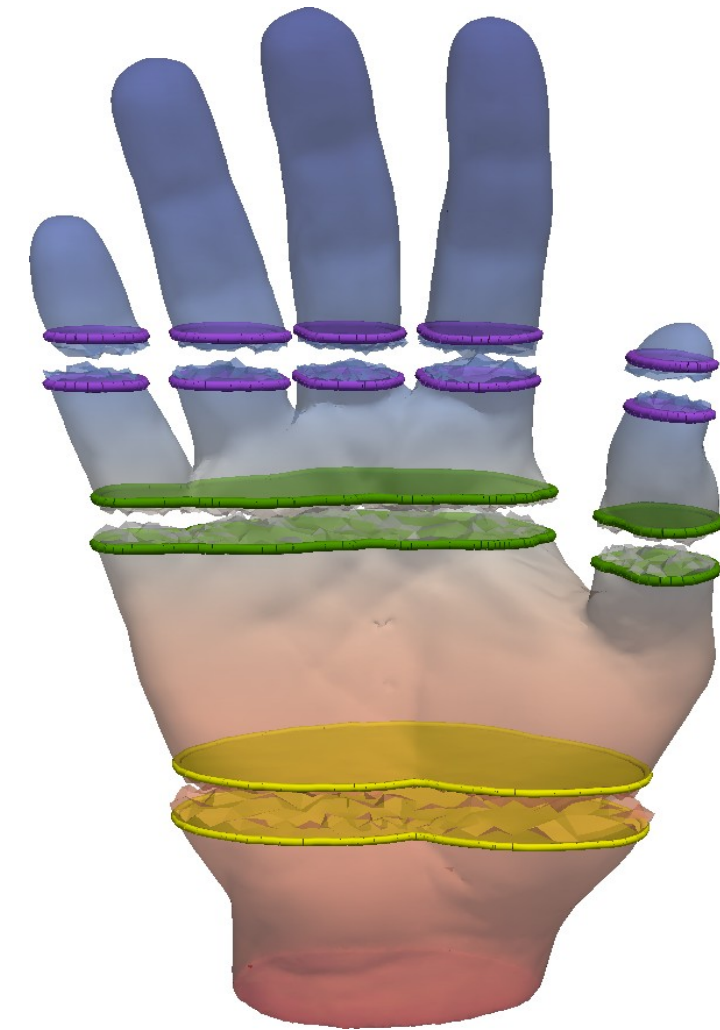
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Redundant computations:

- Extended partition:
initial partition + boundary vertices
- Correct tree in initial partition
- Visit all edges in parallel



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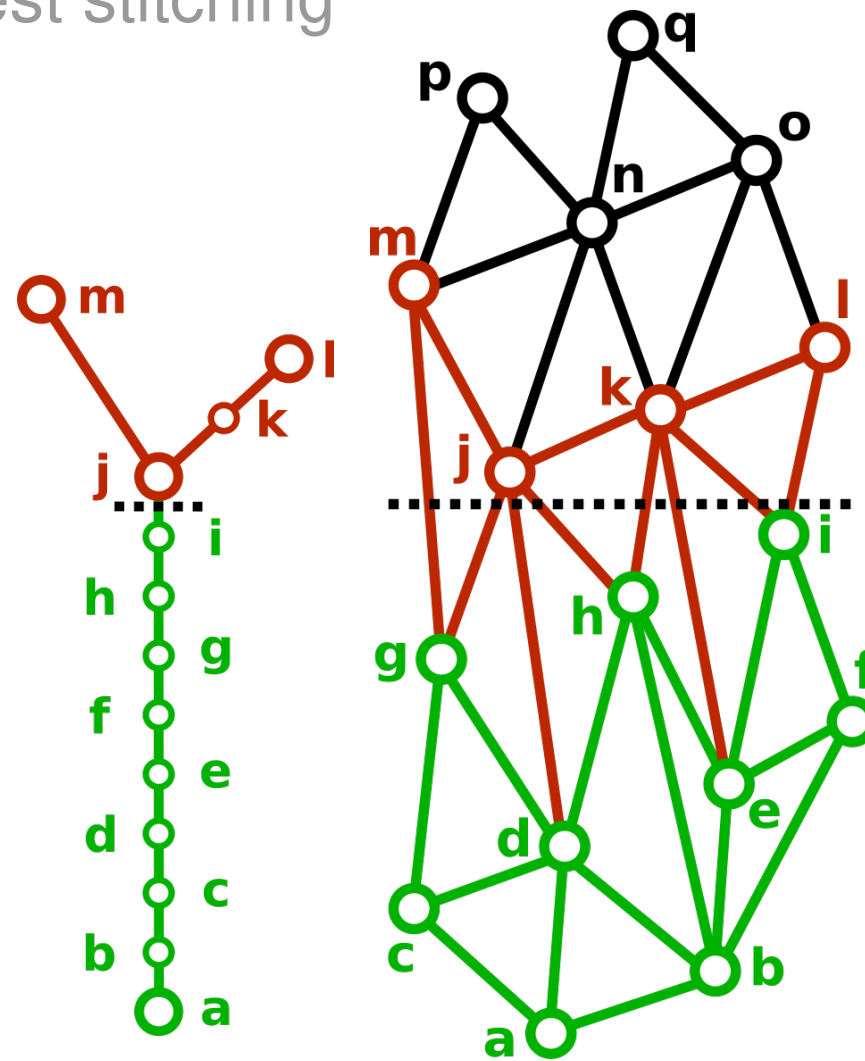


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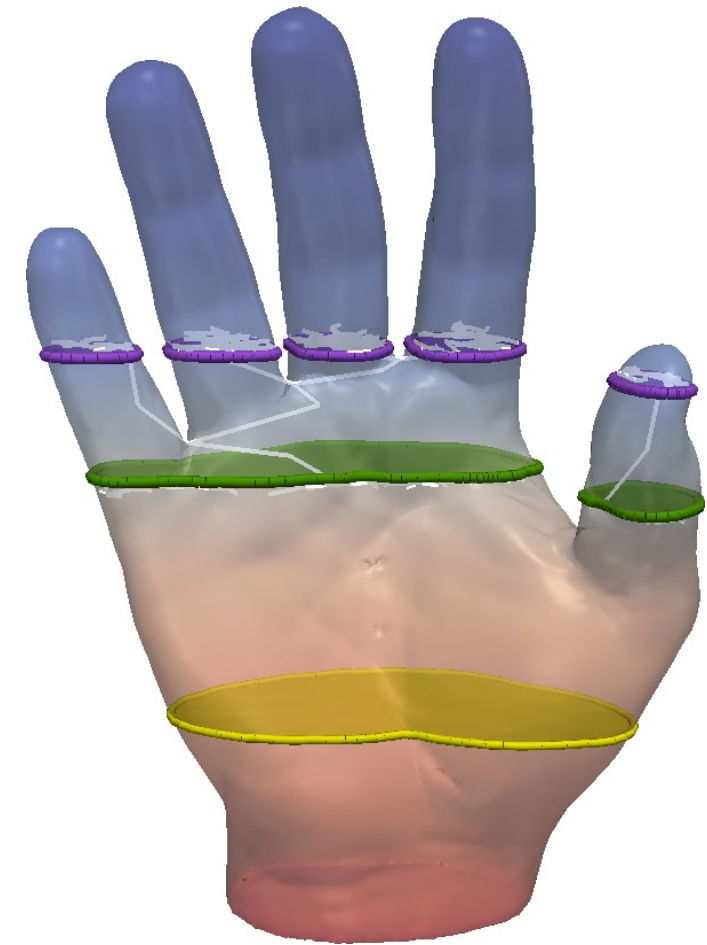
Algorithm

- Domain partitioning
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- In extended partitions
- Using Carr *et al.* Algorithm:
 - Join Tree
 - Split TreeIndependent
- Combination
- Union-Find [CormenItA01]



2D Example



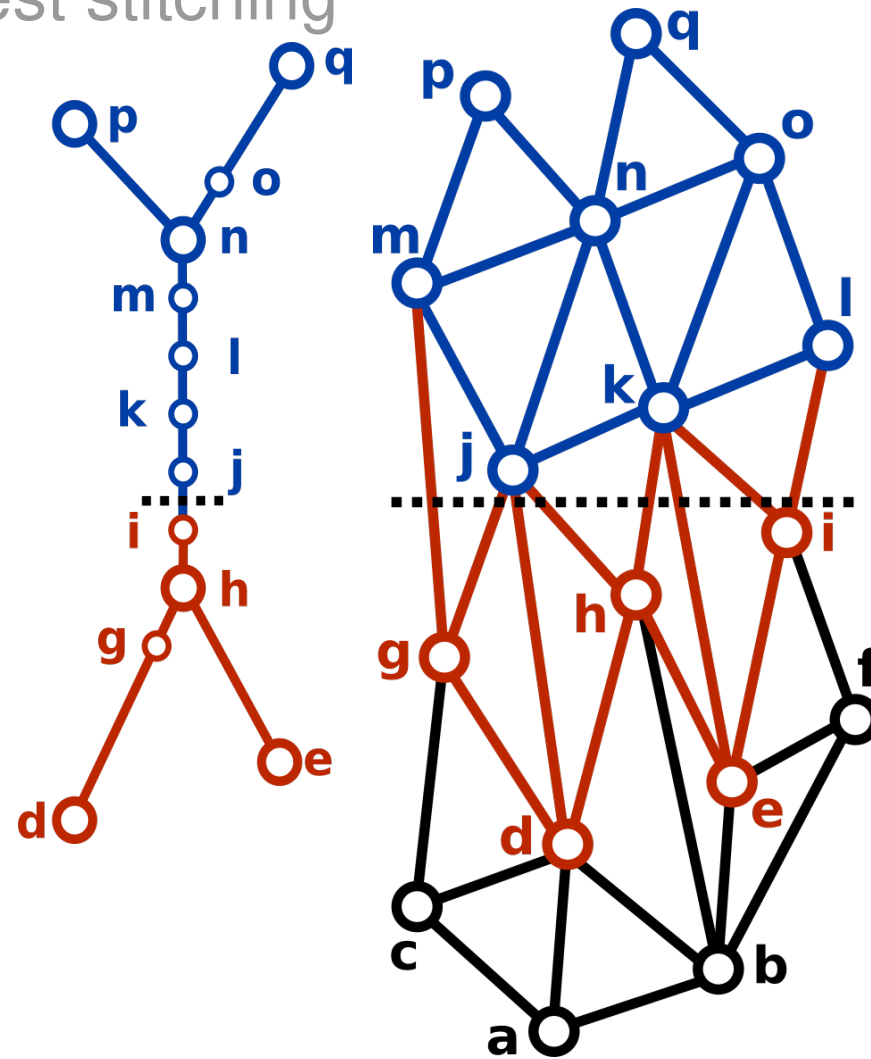
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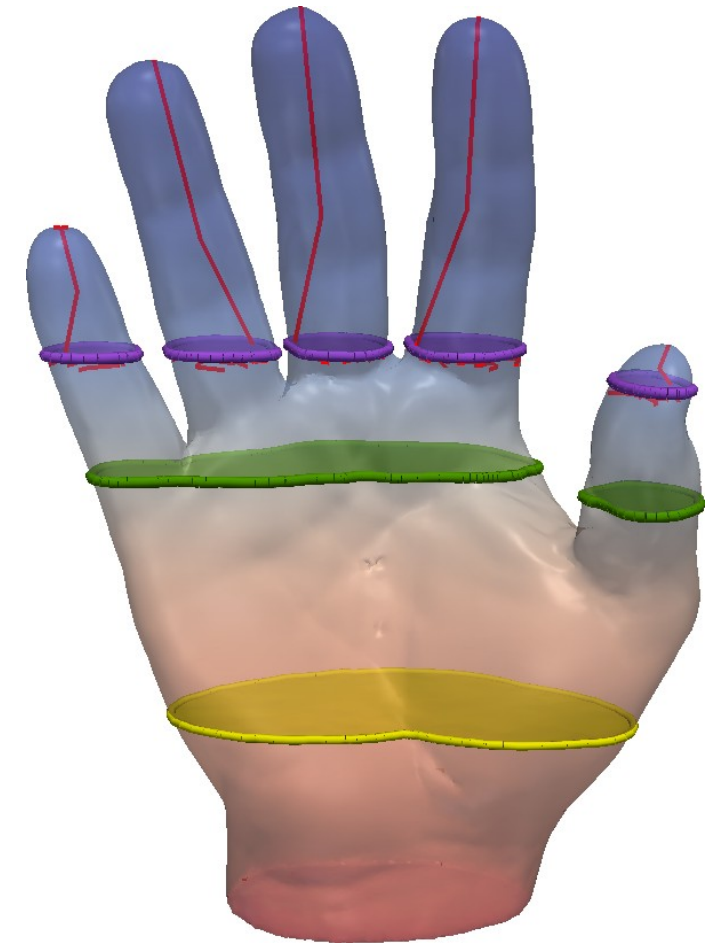
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Each partition:

- Join and Split trees: 2 threads
- Combine: 1 thread
- $O(|\sigma^i| \times \alpha(|\sigma^i|)) + O(|\mathcal{C}(f)|)$
- Keep arcs on the boundary (n-h)



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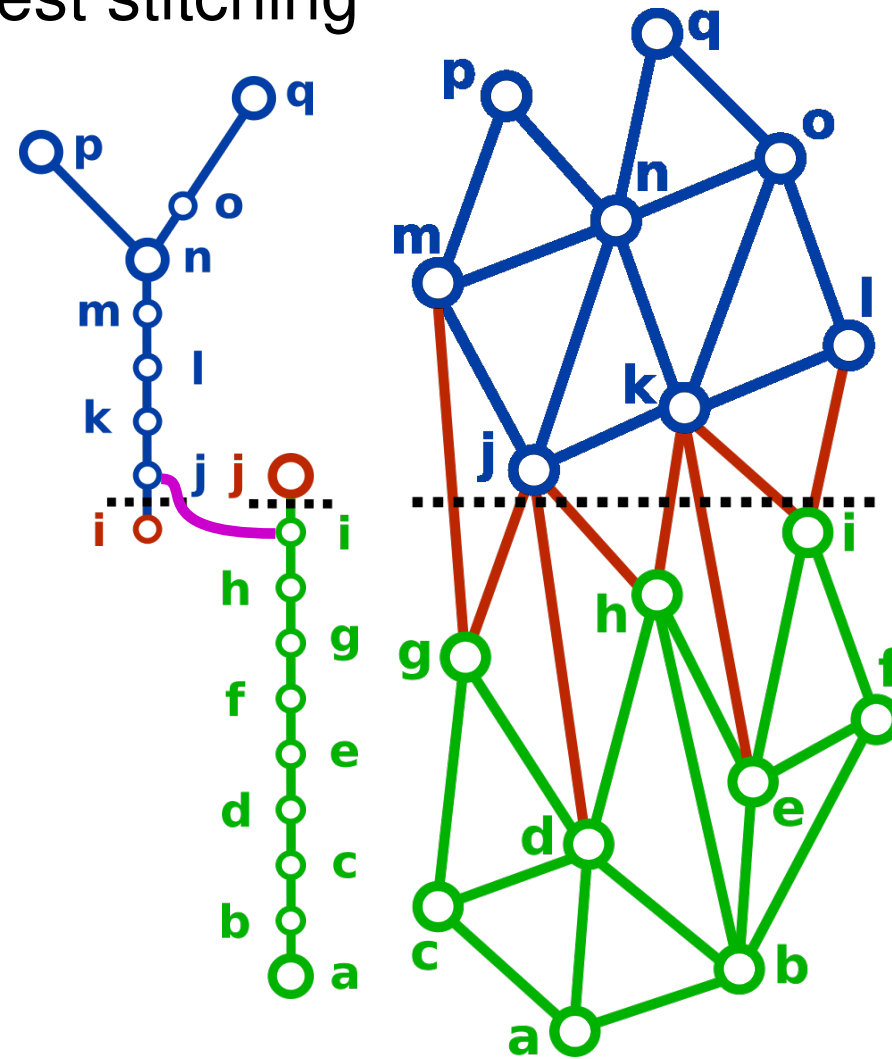


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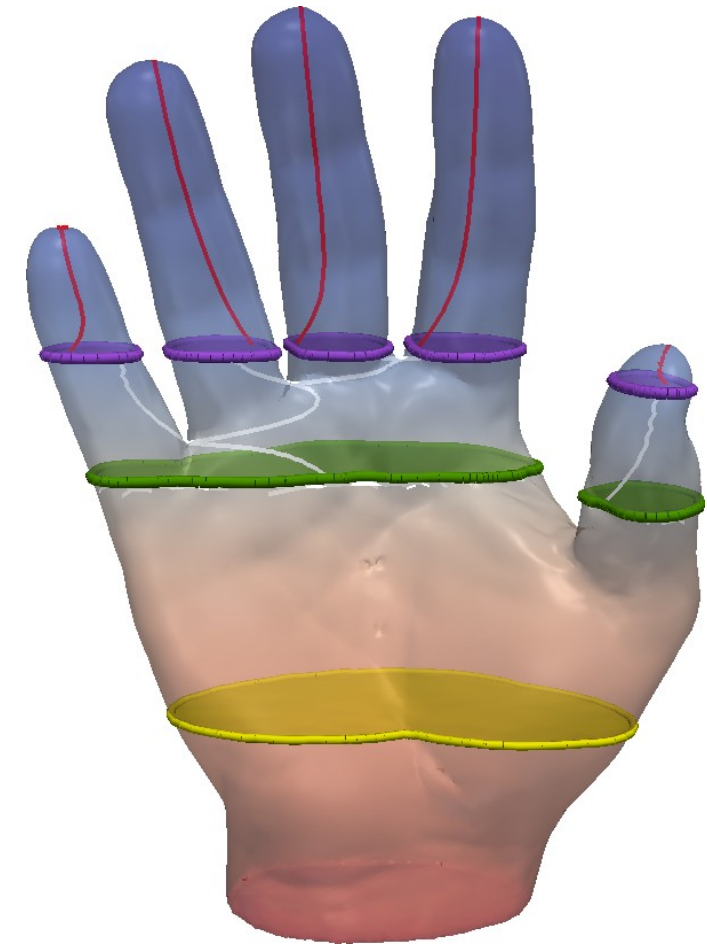
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- Simple step
- Visit crossing arcs
- Cut *interface* arcs
 - Segmentation: fast lookup



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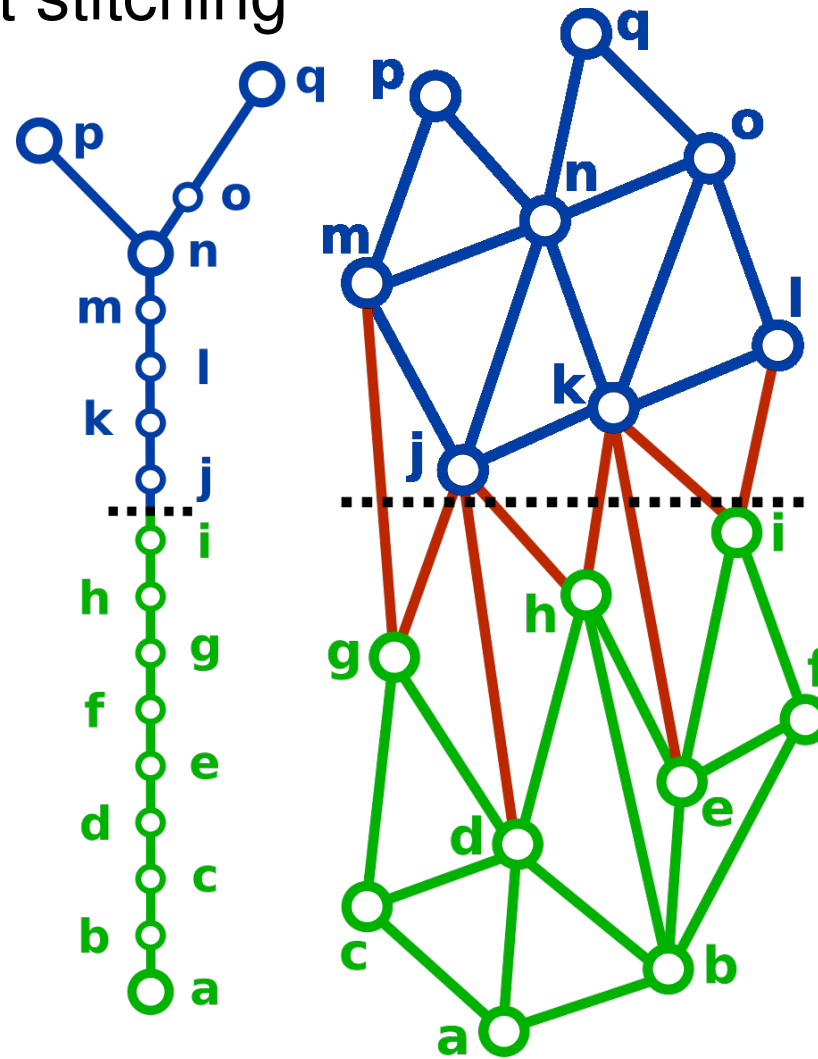


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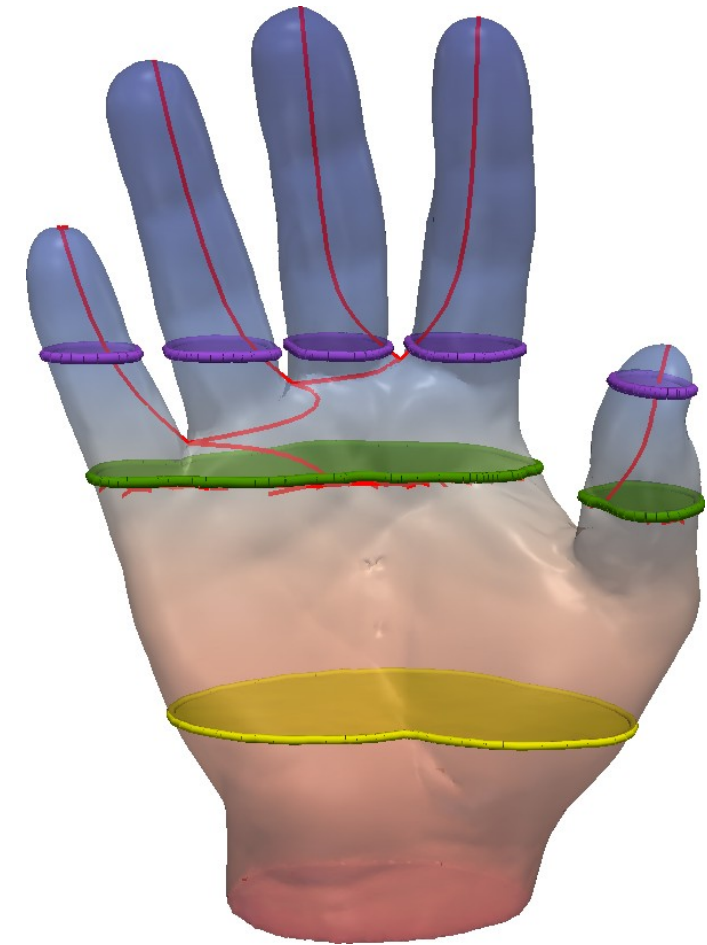
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- New super-arc:
 - Union of the two facing halves
- Once per connected component of level set (\sim crossing arc)



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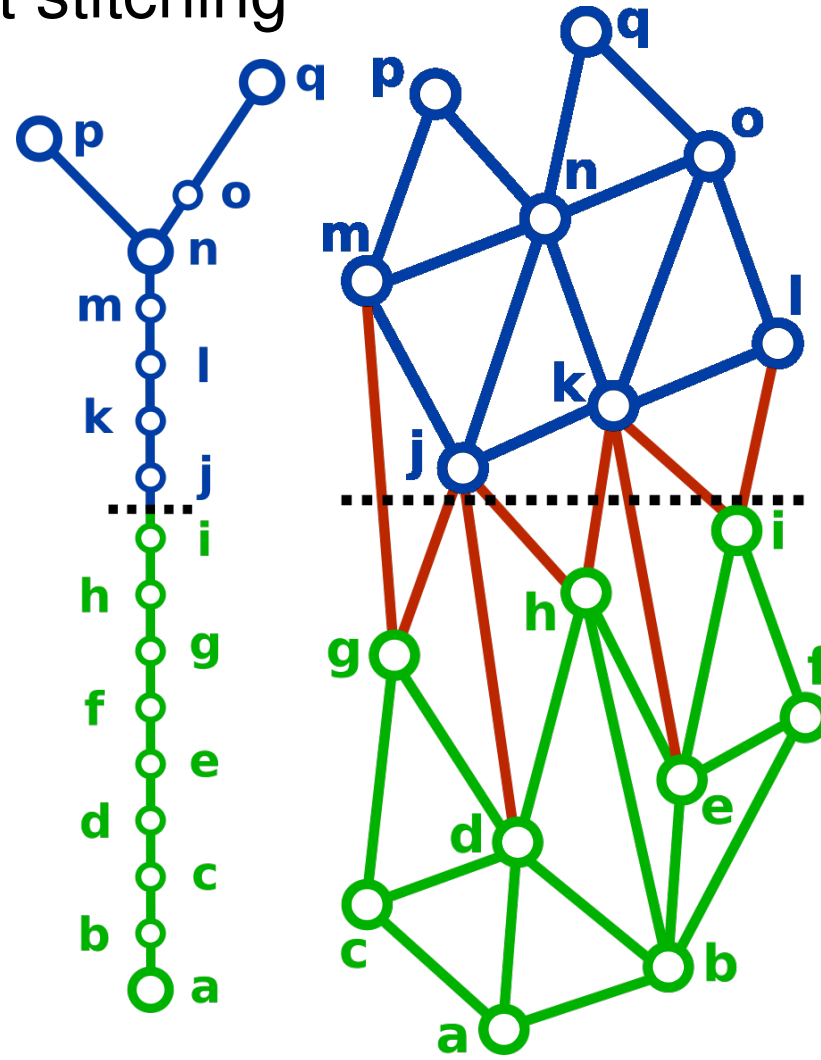


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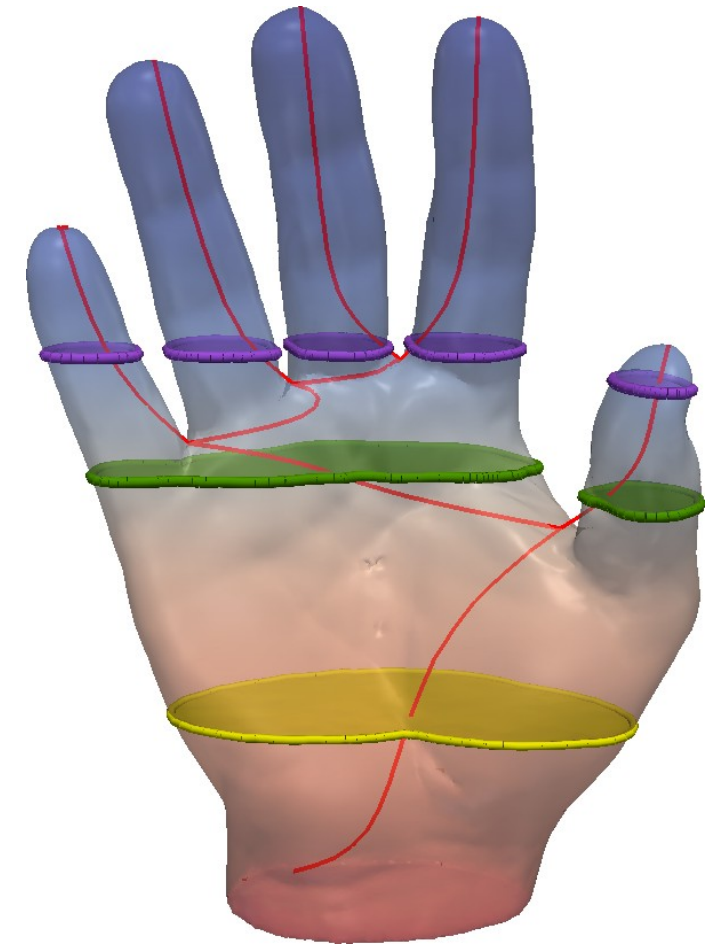
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- Repeat for each interface
- Fast in practice



2D Example



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Experimental results

Intel Xeon CPU E5-2630 v3 (2.4 Ghz, 8 cores)

64GB of RAM

C++ (GCC-4.9), VTK, OpenMP (additional material)

Exp. Results

- Efficiency
- Comparison
- Speed
- Pros & cons

8 threads, 4 partitions

| Data-set | $ \mathcal{M} $ | $ \mathcal{C}(f) _A$ | Sequential | Sort | Overlap | Local trees | Stitching | Overall | Speedup |
|---------------|-----------------|----------------------|------------|------|---------|-------------|-----------|---------|-------------|
| Elevation | 82,906,875 | 1 | 29.18 | 0.91 | 0.18 | 4.18 | 0.14 | 5.42 | 5.38 |
| EthaneDiol | 82,906,875 | 29 | 33.09 | 0.67 | 0.33 | 6.64 | 0.14 | 7.81 | 4.37 |
| Combustion | 82,906,875 | 3649 | 28.04 | 0.61 | 0.34 | 6.19 | 0.15 | 7.31 | 3.83 |
| Boat | 82,906,875 | 3235 | 29.94 | 0.69 | 0.41 | 6.17 | 0.14 | 7.44 | 4.02 |
| Jet | 82,906,875 | 4171 | 26.82 | 0.65 | 0.36 | 6.03 | 0.15 | 7.21 | 3.72 |
| Enzo | 82,906,875 | 282800 | 39.63 | 0.74 | 1.50 | 9.48 | 0.66 | 12.40 | 3.20 |
| Foot | 82,906,875 | 844463 | 18.09 | 0.49 | 0.99 | 7.12 | 1.10 | 9.72 | 1.86 |
| Plasma | 1,310,720 | 2851 | 0.18 | 0.01 | 0.01 | 0.06 | 0.01 | 0.09 | 2 |
| Bucky | 1,250,235 | 4377 | 0.11 | 0.01 | 0.01 | 0.05 | 0.01 | 0.08 | 1.38 |
| SF Earthquake | 2,067,739 | 11887 | 0.19 | 0.01 | 0.02 | 0.09 | 0.02 | 0.13 | 1.46 |

- Uniform sampling

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- Foot: fast computation

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- Overlap and Stitching: efficient

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- High range of value

Exp. Results

- Efficiency
- Comparison
- Speed
- Pros & cons

8 threads, 4 partitions

| Data-set | $ \mathcal{M} $ | $ \mathcal{C}(f) _A$ | Sequential | Sort | Overlap | Local trees | Stitching | Overall | Speedup |
|---------------|-----------------|----------------------|------------|------|---------|-------------|-----------|---------|-------------|
| Elevation | 82,906,875 | 1 | 29.18 | 0.91 | 0.18 | 4.18 | 0.14 | 5.42 | 5.38 |
| EthaneDiol | 82,906,875 | 29 | 33.09 | 0.67 | 0.33 | 6.64 | 0.14 | 7.81 | 4.37 |
| Combustion | 82,906,875 | 3649 | 28.04 | 0.61 | 0.34 | 6.19 | 0.15 | 7.31 | 3.83 |
| Boat | 82,906,875 | 3235 | 29.94 | 0.69 | 0.41 | 6.17 | 0.14 | 7.44 | 4.02 |
| Jet | 82,906,875 | 4171 | 26.82 | 0.65 | 0.36 | 6.03 | 0.15 | 7.21 | 3.72 |
| Enzo | 82,906,875 | 282800 | 39.63 | 0.74 | 1.50 | 9.48 | 0.66 | 12.40 | 3.20 |
| Foot | 82,906,875 | 844463 | 18.09 | 0.49 | 0.99 | 7.12 | 1.10 | 9.72 | 1.86 |
| Plasma | 1,310,720 | 2851 | 0.18 | 0.01 | 0.01 | 0.06 | 0.01 | 0.09 | 2 |
| Bucky | 1,250,235 | 4377 | 0.11 | 0.01 | 0.01 | 0.05 | 0.01 | 0.08 | 1.38 |
| SF Earthquake | 2,067,739 | 11887 | 0.19 | 0.01 | 0.02 | 0.09 | 0.02 | 0.13 | 1.46 |

- About ten seconds

Exp. Results

- Efficiency
- Comparison
- Speed
- Pros & cons

8 threads, 4 partitions

| Data-set | $ \mathcal{M} $ | $ \mathcal{C}(f) _A$ | Sequential | Sort | Overlap | Local trees | Stitching | Overall | Speedup |
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- Parallel efficiency max: 67% (speedup / n_t)
- Parallel efficiency: 40 ~ 55 % (except extrema)

Exp. Results

- Efficiency
- Comparison
- Speed
- Pros & cons

Libtourtre:

- Open-source reference implementation
- pTourtre: naive parallel version

| Data-set | sTourtre | pTourtre | Speedup wrt. | | | |
|---------------|----------|----------|--------------|----------|------|------|
| | | | sTourtre | pTourtre | | |
| Elevation | 20.63 | 10.07 | 2.04 | 5.42 | 3.81 | 2.64 |
| EthaneDiol | 23.47 | 13.96 | 1.68 | 7.81 | 3.00 | 1.79 |
| Combustion | 21.26 | 12.39 | 1.72 | 7.31 | 2.91 | 1.70 |
| Boat | 23.26 | 12.52 | 1.85 | 7.44 | 3.13 | 1.68 |
| Jet | 20.60 | 11.50 | 1.79 | 7.21 | 2.86 | 1.60 |
| Enzo | 32.51 | 18.07 | 1.80 | 12.40 | 2.62 | 1.46 |
| Foot | 13.52 | 8.40 | 1.60 | 9.72 | 1.39 | 0.86 |
| Plasma | 0.08 | 0.08 | 1.00 | 0.09 | 0.89 | 0.89 |
| Bucky | 0.07 | 0.06 | 1.16 | 0.08 | 0.88 | 0.75 |
| SF Earthquake | 0.12 | 0.10 | 1.20 | 0.13 | 0.92 | 0.77 |

Exp. Results

- Efficiency
- Comparison
- Speed
- Pros & cons

| Data-set | sTourtre | pTourtre | Speedup wrt. | Ours | Speedup wrt. | |
|---------------|----------|----------|--------------|-------|--------------|----------|
| | | | sTourtre | | sTourtre | pTourtre |
| Elevation | 20.63 | 10.07 | 2.04 | 5.42 | 3.81 | 2.64 |
| EthaneDiol | 23.47 | 13.96 | 1.68 | 7.81 | 3.00 | 1.79 |
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| Bucky | 0.07 | 0.06 | 1.16 | 0.08 | 0.88 | 0.75 |
| SF Earthquake | 0.12 | 0.10 | 1.20 | 0.13 | 0.92 | 0.77 |

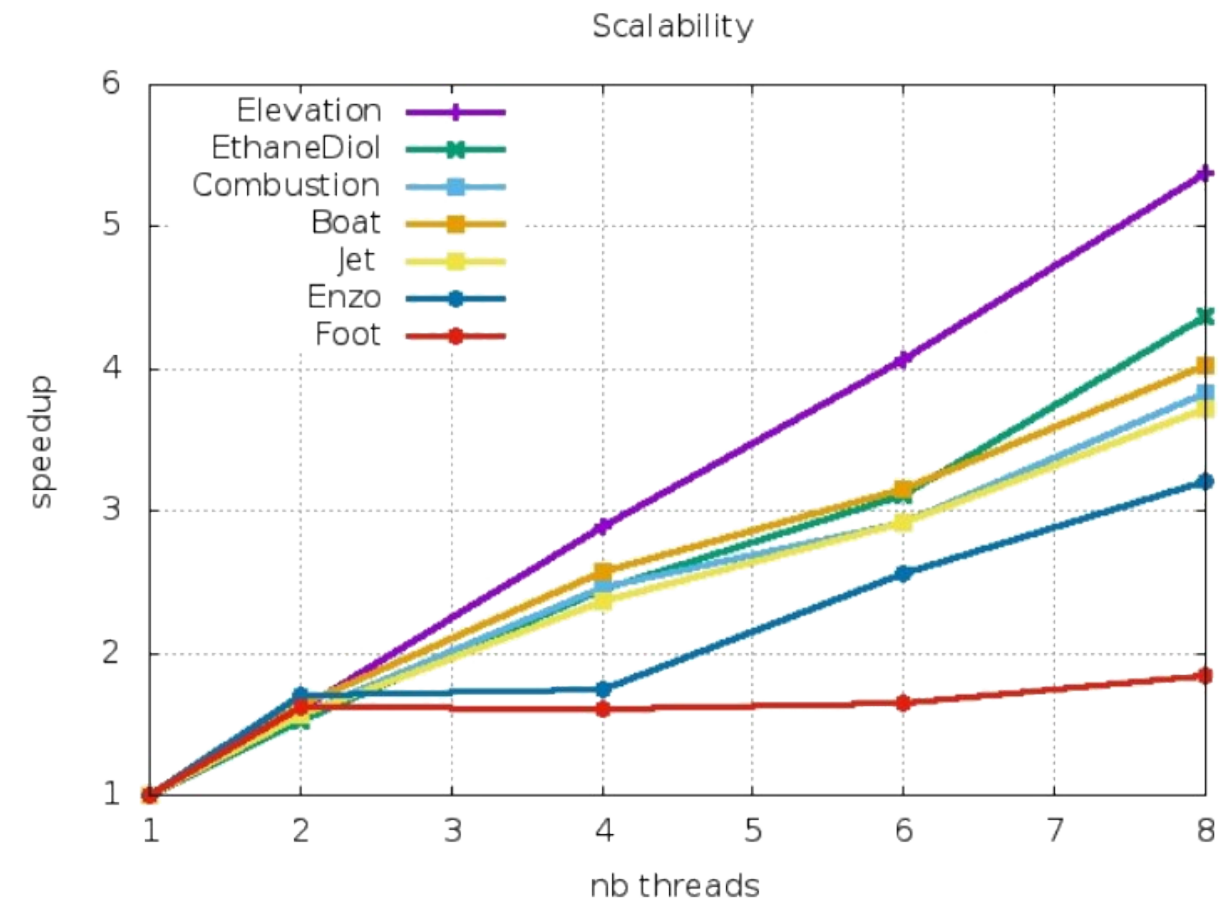
Libtourtre:

- Open-source reference implementation
- pTourtre: naive parallel version
- Always better than sequential libtourtre for big data sets
- Better than parallel except for the foot data set

Exp. Results

- Efficiency
- Comparison
- Speed
- Pros & cons

- Different slopes
- Few arithmetic operations per memory access

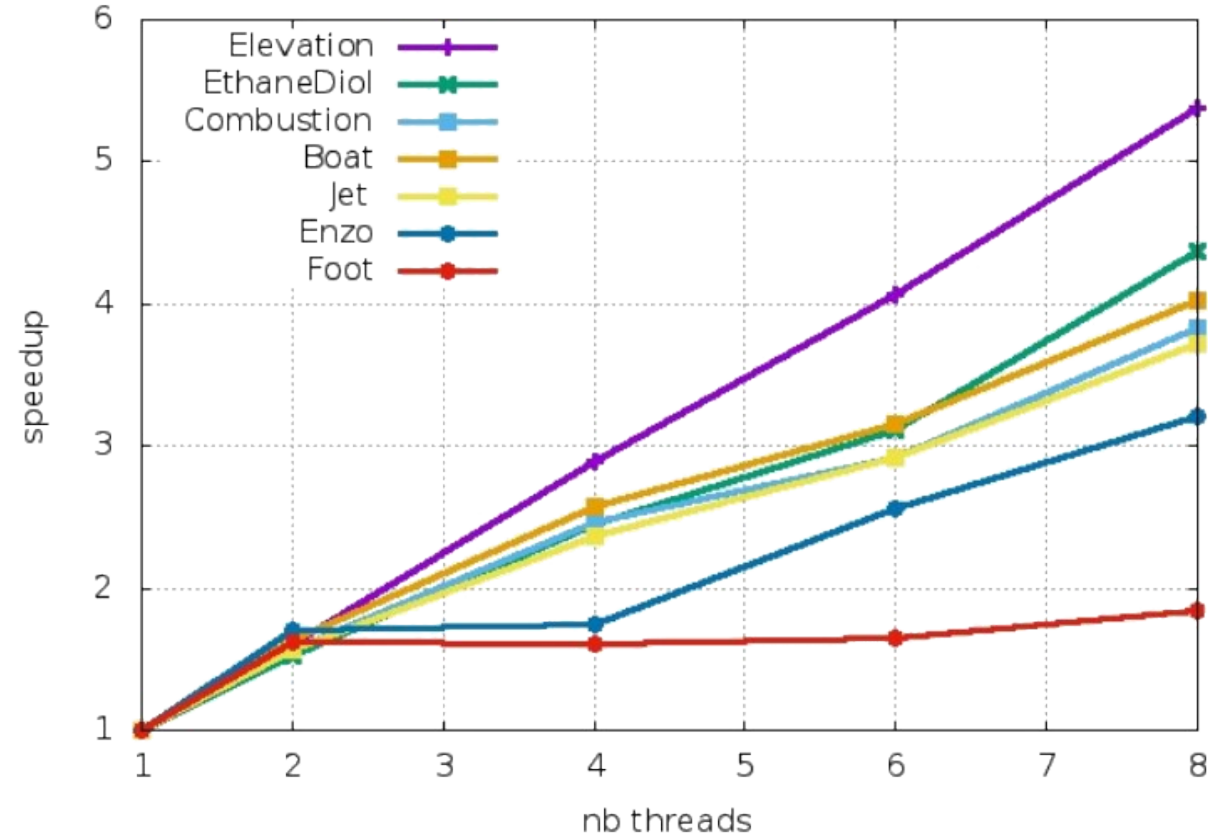


Exp. Results

- Efficiency
- Comparison
- Speed
- Pros & cons

- Different slopes
- Few arithmetic operations per memory access
- Load imbalance

Scalability



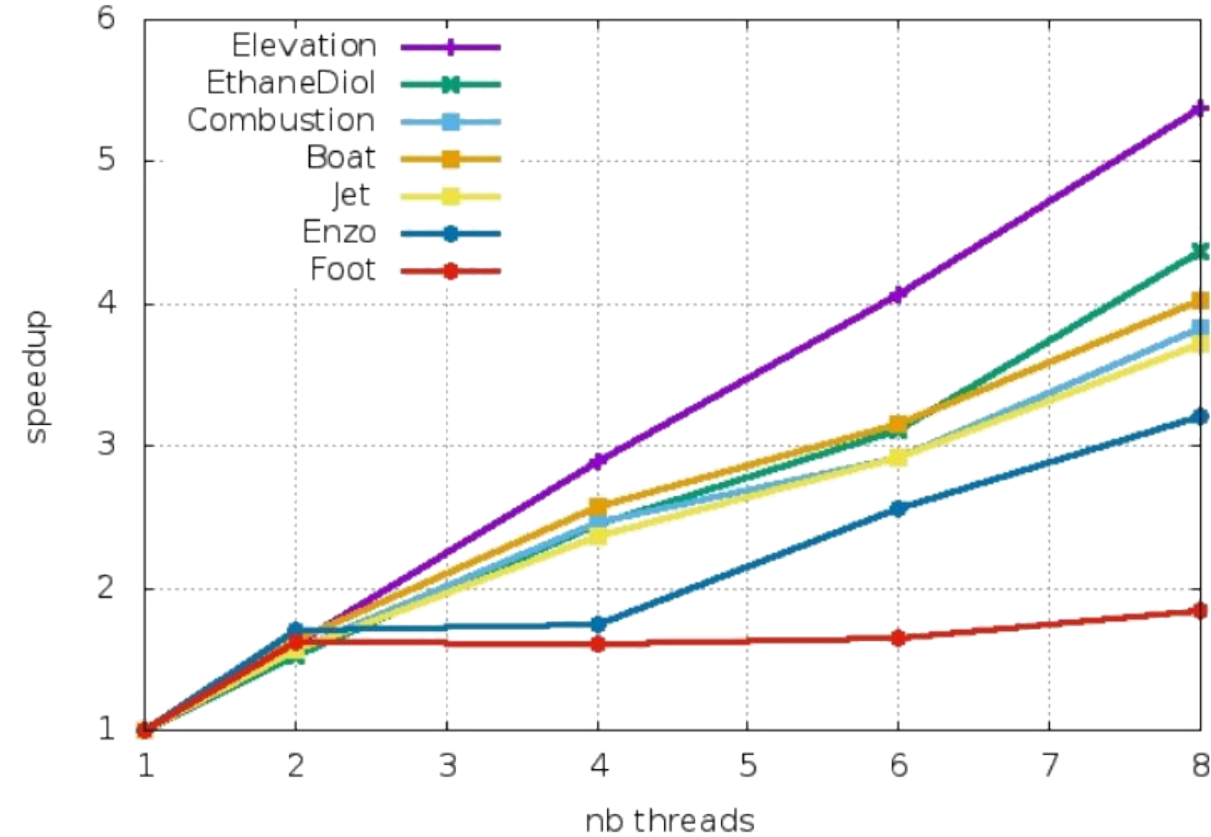
| Data-set | Parallel: min | max | 1 thread: min | max |
|------------|---------------|-----------|---------------|-----------|
| Elevation | 1,623,500 | 1,768,720 | 2,151,250 | 2,292,390 |
| EthaneDiol | 963,962 | 1,108,170 | 1,470,960 | 1,804,410 |
| Combustion | 1,029,050 | 1,190,160 | 1,688,080 | 2,006,210 |
| Boat | 1,055,410 | 1,237,030 | 1,463,880 | 1,985,720 |
| Jet | 1,065,720 | 1,256,730 | 1,754,240 | 2,094,010 |
| Enzo | 860,937 | 933,616 | 1,166,540 | 1,366,070 |
| Foot | 1,120,560 | 4,031,030 | 1,220,800 | 5,195,250 |

Computational speed: vertices/second

Exp. Results

- Efficiency
- Comparison
- Speed
- Pros & cons

Scalability



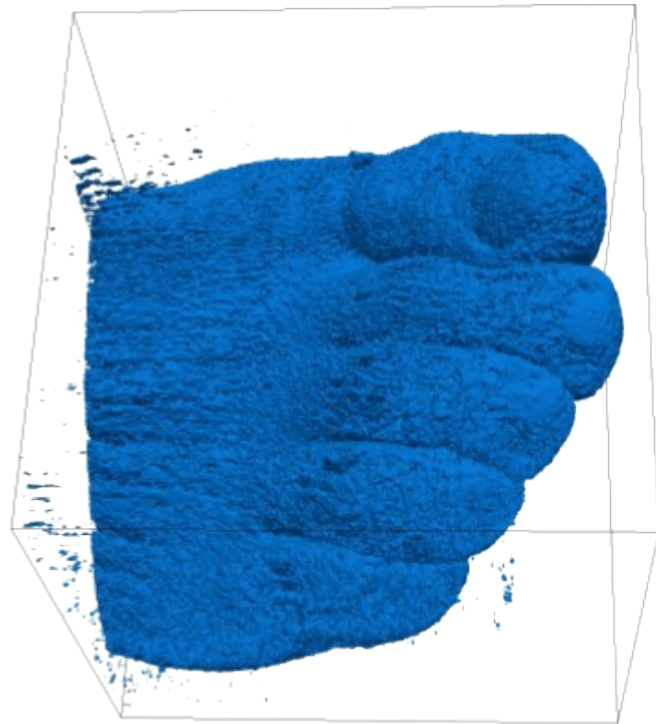
- Different slopes
- Few arithmetic operations per memory access
- Load imbalance
- Memory congestion

| Data-set | Parallel: min | max | 1 thread: min | max |
|------------|---------------|-----------|---------------|-----------|
| Elevation | 1,623,500 | 1,768,720 | 2,151,250 | 2,292,390 |
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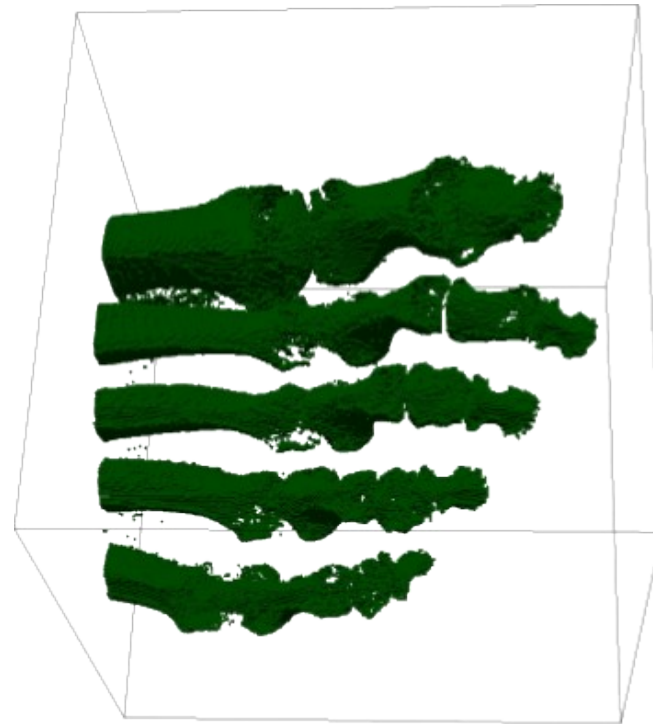
Computational speed: vertices/second

Exp. Results

- Efficiency
- Comparison
- Speed
- Pros & cons



(a)



(b)

- Different slopes
- Few arithmetic operations per memory access
- Load imbalance
- Memory congestion
- Redundant computations

| Data-set | ideal | min | max |
|------------|-----------|-----------|-----------|
| Elevation | 4,194,304 | 4,259,840 | 4,325,376 |
| EthaneDiol | 4,194,304 | 4,362,086 | 4,616,938 |
| Combustion | 4,194,304 | 4,353,986 | 4,635,078 |
| Boat | 4,194,304 | 4,418,409 | 4,791,092 |
| Jet | 4,194,304 | 4,358,176 | 4,701,586 |
| Enzo | 4,194,304 | 5,234,144 | 6,474,322 |
| Foot | 4,194,304 | 4,499,572 | 6,044,708 |

Partitions sizes in vertices

Exp. Results

- Efficiency
- Comparison
- Speed
- Pros & cons

Pros:

- Good parallel efficiency
- Faster than reference implementation
- Large spectrum of data

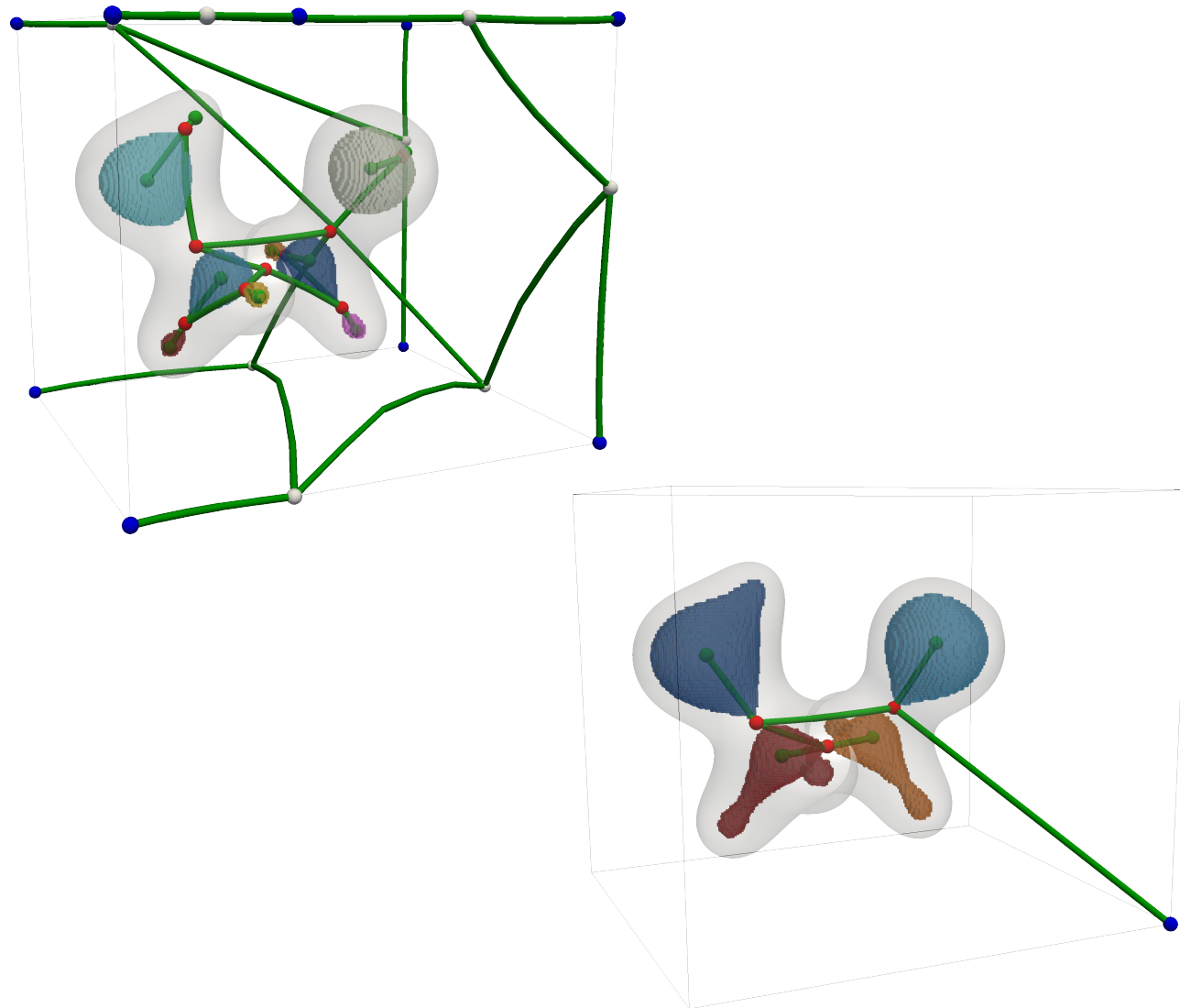
Cons:

- Redundant computation
- Load imbalance
- Memory congestion (augmented tree)



Application

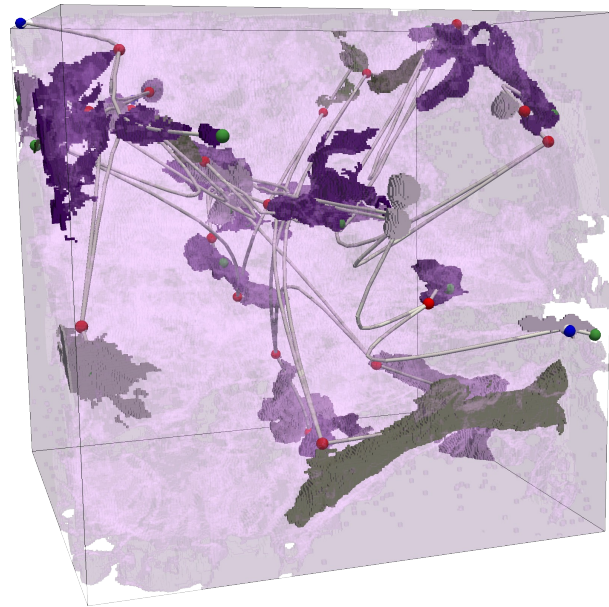
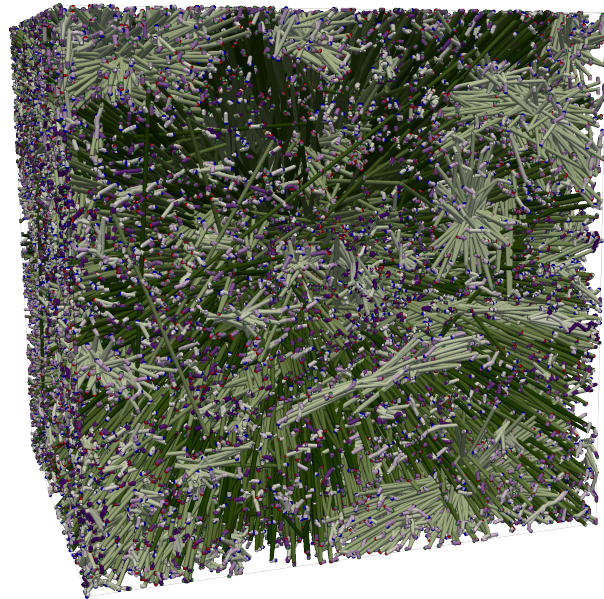
Application



Exploration:


- Highlight features
- Allows features grouping

Application



Occlusion reduction:

- Remove noise
- Keep the most important features



Conclusion

Conclusion

- Recall
- Perspective

Take home message:

- Efficient algorithm:
 - Multi-threaded
 - Augmented
 - Simple approach, subtle details

Conclusion

- Recall
- Perspective

Take home message:

- Efficient algorithm:
 - Multi-threaded
 - Augmented
 - Simple approach, subtle details

- VTK-based implementation:
 - Generic input
 - VTU, VTI
 - 2D/3D
 - Generic output (augmented trees)
 - Ready-to-use
 - Integrated in TTK

Conclusion

- Recall
- Perspective

Take home message:

- Efficient algorithm:
 - Multi-threaded
 - Augmented
 - Simple approach, subtle details

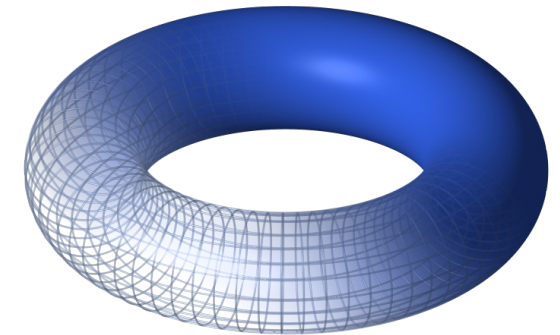
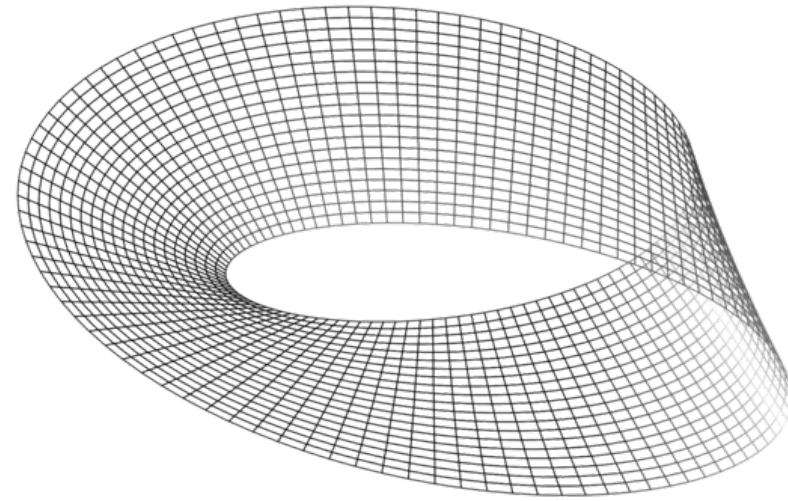
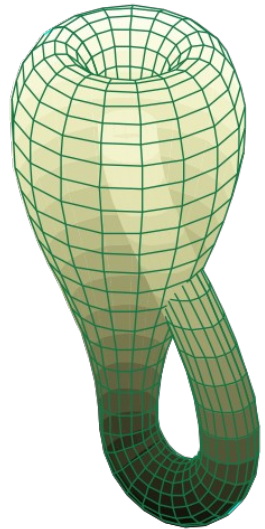
- VTK-based implementation:
 - Generic input
 - VTU, VTI
 - 2D/3D
 - Generic output (augmented trees)
 - Ready-to-use
 - Integrated in TTK
- Lesson learned
 - Memory bound
 - Memory congestion: price to pay for augmented trees
 - Efficient implementation: hard

Conclusion

- Recall
- Perspective

- Improve partitioning:
 - Better cutting isovalue selection
 - Contour Spectrum
- Distributed systems

The end



Thank you for your attention,
Do you have any question ?

Paper at: <http://www-pequan.lip6.fr/~tierny/>

Code at: <https://github.com/topology-tool-kit/ttk>

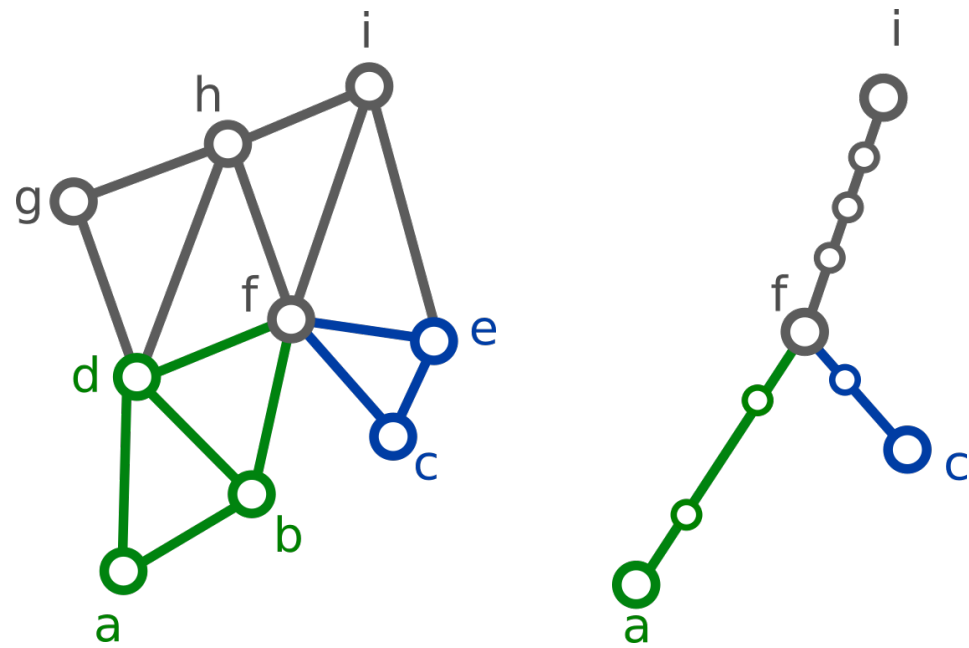
This work is partially supported by the Bpifrance grant “AVIDO” (Programme d’Investissements d’Avenir, reference P112017-2661376/DOS0021427) and by the French National Association for Research and Technology (ANRT), in the framework of the LIP6 - Kitware SAS CIFRE partnership reference 2015/1039.



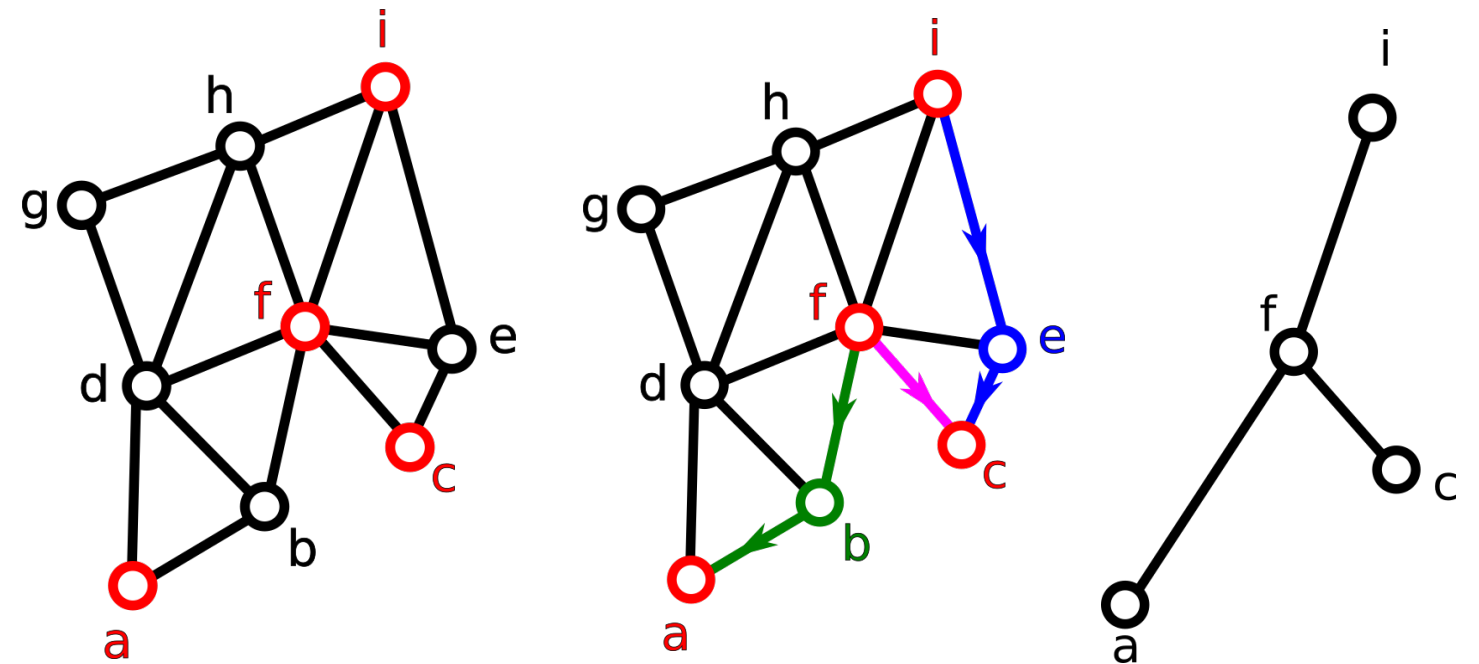
Appendice

Seq. Approaches

Union find:



Monotone paths:



Critical points

